High Temperature Low Cycle Fatigue Data for Three High Strength Nickel-Base Superalloys.

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This report presents a summary of the high temperature low cycle fatigue data for three high strength nickel-base superalloys, Rene 95, AP-115, and AV2-10A. The majority of tests were performed in strain control at 1200°F and 1400°F, and at frequencies of 20 cpm, 0.2 cpm, and 0.05 cpm. Conventional triangular waveform was used for most of the testing although strain dwell tests and some SLOO-FAST and FAST-SLOW tests were also included.
The primary purpose of this report is to make these data available in the literature. Some analyses and interpretation of the data are also included along with an original format for data presentation in terms of stress amplitude and mean stress.
FOREWORD

This technical report summarizes the high temperature low cycle fatigue testing accomplished by Mar-Test Inc., under Materials Laboratory contract F33615-76-C-5245, "High Temperature Testing". The work reported herein was performed during the period 1 June 75 through 1 January 1979 under the direction of Capt. Jack Hyeak (AFWAL/MLN), contract monitor. Henry L. Bernstein of Systems Research Laboratories also contributed significantly to the design and evaluation of this test program under AFWAL/ML contract F33615-76-C-5191, "Mechanical Property Testing and Material Evaluation".

Special thanks are also to be extended to Ms. Debbie Magee and Ms. Karen Cassidich-Swango for their assistance in the preparation of the manuscript.

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</tbody>
</table>
SECTION I
INTRODUCTION

A major area of concern in the development of recent military turbine engines has been life cycle management. A part of the technology needed to optimize the life of components, such as turbine disks, is the ability to accurately predict their crack initiation lives under typical cyclic conditions. With the increasing turbine temperatures that accompany performance gains, the turbine section operating conditions are becoming increasingly severe. Typical military flight missions include significant dwell periods at high power settings with the result that time dependent damage mechanisms operate. This has necessitated modification of existing life relationships previously relied upon at lower temperature.

Programs have been initiated at the Materials Laboratory and in industry to develop analytical models for predicting crack initiation in nickel-base superalloys under creep-fatigue conditions. As part of the effort, this work was initiated to provide a substantive low cycle fatigue database for alloys of particular interest to the Air Force. The alloys that have been tested extensively under this program are cast and wrought Rene 95, a current turbine disk alloy rated for 1200°F service, and AF-115 and AF2-1DA, powder metallurgy superalloys being developed for 1600°F use. The test matrix has been designed to study the effect of cyclic frequency and dwell period and it has been necessarily limited to the primary service temperature for each alloy. Where possible, additional waveforms and temperatures have been included.

The major emphasis of this report is on data presentation. A complete summary of all the fatigue tests is present in Tables 1 through 5. Some analysis and interpretation of data trends have also been included.
The evaluations of the data focus on attempts to identify mathematical models for certain materials behavior. An original format for data presentation in terms of stress amplitude and mean stress is described.

The data generated in this program have been the basis for three AFML Technical Reports, (2,3,12) and have been included in the proceedings of an AGARD panel meeting. 4 An extensive review of the analytical models for predicting LCF crack initiation at elevated temperature is the subject of one of the AFML Technical Reports. 2 Another AFML Technical Report gives the behavior of the stresses during many of the fatigue tests. 12
SECTION II
MATeRIALS

1. AP-115

a. Processing

Two vacuum induction melted ingot master heats, V03963 and V03964 were made in the Carpenter Technology Corporation R&D Center. The chemistries of these heats are shown in Table 1. The VIM master heats were vacuum induction remelted as a single atomization heat, A844, which was subsequently argon atomized. The chemistry of this heat is also shown in Table 1.

Type 304SS canisters were prepared and powder was charged into canisters (O646 and C655) under vacuum less than 5 microns Hg. The canisters were compacted in two separate HIP cycles #1474 and #1477 using Industrial Materials Technology Corporation’s 8” x 26” National Forge Unit. The pressing parameters used were 2175°F/2 Hrs./15 ksi.

Subsequent to compaction, canister O646 was cut into 10 slices. Slices #3, #5, and #8 were then forged by the Wyman-Gordon Company prior to heat treatment. The forging practice involved using die shocks heated to 1650-2100°F at a press head velocity of 1 to 5 inches/minute. A total reduction of 50% was accomplished.

All ten pancakes (3 forged plus 7 as HIP) were solution-treated at a temperature of 2175°F (+10, -25) for four hours followed by a fan air-cool. The aging treatment was 1425°F (+25) for 16 hours followed by an air-cool. The tensile properties of AP-115 in both the HIP and HIP plus forge conditions are summarized in Table 2.
b. Microstructure

The AF-115 alloy was studied in the HIP and heat treated, as well as the HIP plus forged and heat treated conditions. The recommended processing parameters for these treatments resulted in a very similar microstructure, that differed significantly only in grain size. The AF-115 microstructure was dominated by three distinct sizes of γ' precipitate. The irregular shaped unsolutioned γ' precipitates were positioned along the grain boundaries and were approximately 3–10μ along their major axis, and the cooling γ' particles which were contained within the grains were cuboidal in shape approximately .25μ on edge. The ultra-fine aging γ' particles were more spherical in shape and had a diameter of .02–.04μ.

AF-115 also contained a small amount of carbides which were approximately 50μ in diameter. The carbides were, in general, uniformly distributed throughout the grain boundaries often lying near the unsolutioned γ' particles. There were observations in isolated areas of carbide particles decorating prior particle boundaries, but this did not appear to be a general problem. Although neither quantitative analysis nor microdiffraction studies were undertaken, the majority of the carbides in AF-115 were believed to be MC type. This was supported by microprobe analysis which indicated that the carbides were rich in MC formers; titanium, columbium, tantalum, and hafnium; and depleted in chromium, a M₂₃C₆ carbide former.

The grain size of the as-HIP AF-115 was ASTM #7.0 (30μ diameter), while the HIP plus forged alloy had a grain size of ASTM #6.5 (19μ diameter). The AF-115 alloy was processed into 10 individual pancakes of material. There was uniformity of microstructure and mechanical properties for all pancakes.
c. Powder Metallurgy Defects

There were three distinct defect types that were found in this heat of AF-115 alloy; pores, nonmetallic inclusions, and hafnium oxide inclusions. Pores were the most populous of the defects. The porosity is a by-product of the powder production process. Argon gas is adsorbed onto the powder surface or entrapped in hollow particles during the argon atomization phase. The gas subsequently expands during the solution heat treatment which results in the porosity. The level of porosity is, therefore, a function of atomization processing and solutioning temperature.

The level of porosity in the AF-115 alloy was quantitatively determined using a thermal induced porosity (TIP) test. This involved measuring the density of a sample of the billet material before and after the solutioning heat treatment. The change in density due to the expansion of the gas at high temperature was a measure of the porosity level.

This heat of AF-115 had a change in density due to thermal induced porosity of .42% after solutioning at 2175°F. This is considered an abnormally high level. The pores ranged in size from a few microns in diameter to approximately 130μ in diameter.

Considerably less populous than the pores was the second most prevalent defect in AF-115, nonmetallic inclusions. These were tramp pieces of ceramic equipment liners used in the powder production process. These inclusions were generally high in concentrations of calcium, silicon, aluminum, and magnesium. These inclusions were up to 100μ in length and ranged from spherical to elliptical in shape. The inclusions were often fractured before fatigue testing and were generally poorly bonded to the matrix.
The final and least populous defect in this heat of AF-115 was the hafnium oxide inclusions (probably $\text{HfO}_2$). These inclusions were plate-like and were up to 125μ in diameter with a thickness of only 3μ. They formed in the melt and were a result of the high hafnium content. $\text{HfO}_2$ particles were normally bonded more strongly to the matrix than the other inclusions.
TABLE 1

AF-115 - CHEMICAL ANALYSES; WT. PERCENT

<table>
<thead>
<tr>
<th>Element</th>
<th>W03963</th>
<th>T03964</th>
<th>A00884</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>.155</td>
<td>.164</td>
<td>.155</td>
</tr>
<tr>
<td>Mn</td>
<td>.01</td>
<td>.01</td>
<td>&lt;.01</td>
</tr>
<tr>
<td>Si</td>
<td>&lt;.01</td>
<td>&lt;.01</td>
<td>.03</td>
</tr>
<tr>
<td>P</td>
<td>&lt;.005</td>
<td>&lt;.005</td>
<td>&lt;.005</td>
</tr>
<tr>
<td>S</td>
<td>.003</td>
<td>.003</td>
<td>.002</td>
</tr>
<tr>
<td>Cr</td>
<td>10.80</td>
<td>11.08</td>
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</tr>
<tr>
<td>Mo</td>
<td>2.86</td>
<td>2.90</td>
<td>2.62</td>
</tr>
<tr>
<td>Co</td>
<td>15.04</td>
<td>15.3C</td>
<td>14.95</td>
</tr>
<tr>
<td>Ti</td>
<td>3.92</td>
<td>3.84</td>
<td>3.90</td>
</tr>
<tr>
<td>Al</td>
<td>4.00</td>
<td>3.79</td>
<td>3.85</td>
</tr>
<tr>
<td>Nb</td>
<td>1.64</td>
<td>1.75</td>
<td>1.62</td>
</tr>
<tr>
<td>W</td>
<td>6.05</td>
<td>6.20</td>
<td>5.62</td>
</tr>
<tr>
<td>B</td>
<td>.022</td>
<td>.023</td>
<td>.023</td>
</tr>
<tr>
<td>Hf</td>
<td>0</td>
<td>0</td>
<td>2.02</td>
</tr>
<tr>
<td>Zr</td>
<td>0</td>
<td>0</td>
<td>.045</td>
</tr>
<tr>
<td>Si</td>
<td>.0006</td>
<td>.0012</td>
<td>.0044</td>
</tr>
<tr>
<td>S</td>
<td>.001</td>
<td>.001</td>
<td>.001</td>
</tr>
<tr>
<td>PANCAKE</td>
<td>TEMP, °F</td>
<td>0.2% YIELD STRENGTH, ksi</td>
<td>UTS, ksi</td>
</tr>
<tr>
<td>-----------</td>
<td>---------</td>
<td>--------------------------</td>
<td>---------</td>
</tr>
<tr>
<td>9 HIP</td>
<td>1400</td>
<td>152.5</td>
<td>172.9</td>
</tr>
<tr>
<td>2 HIP</td>
<td>1400</td>
<td>143.5</td>
<td>167.7</td>
</tr>
<tr>
<td>7 HIP</td>
<td>1400</td>
<td>146.9</td>
<td>273.4</td>
</tr>
<tr>
<td>9 HIP</td>
<td>1500</td>
<td>135.4</td>
<td>146.5</td>
</tr>
<tr>
<td>HIP/Forge</td>
<td>1400</td>
<td>150.8</td>
<td>164.2</td>
</tr>
<tr>
<td>5 HIP/Forge</td>
<td>1400</td>
<td>151.0</td>
<td>168.8</td>
</tr>
</tbody>
</table>
2. **AP2-1DA**

a. **Processing**

The two AP2-1DA pancakes (B1 and B2) used for this study were produced from federal Mogal Inc. powder Heat 454. The composition of the powder is contained in Table 3. The powder was 100 mesh argon atomized.

The powder was sealed in a stainless steel can and compacted at 2000°F ± 25°F at 30,000 psi for 21 seconds. The compact was then extruded at 2025°F ± 25°F. The reduction ratio was 7.3 to 1.0. After extrusion, the compact was superplastically forged at 2025°F ± 15°F, at a strain rate of 0.1 in/3s/min.

The forgings were finally heat treated by the following sequence:

1) 2210°F ± 15°F/2 Hrs./Air Cool
2) 2050°F ± 15°F/2 Hrs./Air Cool
3) 1300°F ± 25°F/8 Hrs./Air Cool
4) 1500°F ± 25°F/8 Hrs./Air Cool

The tensile properties of AP2-1DA are summarized in Table 4.
b. Microstructure

The AP2-1DA microstructure also had three sizes of γ' precipitate. An irregular shaped primary γ' (1-3 μ) decorated the grain boundaries with cuboidal cooling γ' (.25μ) and aging γ' (.06-.08μ) contained within the grains.

Due to the higher carbon content, there were more carbides in the AP2-1DA microstructure than in AP-115. The carbides were again rich in MC carbide formers, and they were evenly dispersed throughout the microstructure.

The grain size for AP2-1DA was relatively large (grain diameter 200μ). Also prevalent within the grains were annealing twins of varying size.
c. P/M Defects

Although the AF2-1DA powder was also made by the argon atomization technique, the processing of this heat of powder was such that there was no significant level of porosity in the forgings. There were also no hafnium oxide inclusions as in the AF-115 alloy. The only defects were nonmetallic inclusions similar to those in the AF-115 alloy. Their size ranges up to 100µ in length.
<table>
<thead>
<tr>
<th>Element</th>
<th>Composition (Wt. Percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cr</td>
<td>12.29</td>
</tr>
<tr>
<td>Ti</td>
<td>2.89</td>
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<tr>
<td>Co</td>
<td>10.10</td>
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<td>W</td>
<td>5.70</td>
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<tr>
<td>Al</td>
<td>4.70</td>
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<td>Mo</td>
<td>3.00</td>
</tr>
<tr>
<td>Ta</td>
<td>1.90</td>
</tr>
<tr>
<td>Mn</td>
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<tr>
<td>Zr</td>
<td>0.084</td>
</tr>
<tr>
<td>Si</td>
<td>&lt; 0.1</td>
</tr>
<tr>
<td>Fe</td>
<td>&lt; 0.1</td>
</tr>
<tr>
<td>B</td>
<td>0.016</td>
</tr>
<tr>
<td>C</td>
<td>0.31</td>
</tr>
<tr>
<td>S</td>
<td>0.007</td>
</tr>
<tr>
<td>P</td>
<td>&lt; 0.002</td>
</tr>
<tr>
<td>O₂</td>
<td>65 PPM</td>
</tr>
</tbody>
</table>

Balance - Nickel
<table>
<thead>
<tr>
<th>PANCAKE</th>
<th>TEMP. °F</th>
<th>0.2% YIELD STRESS (ksi)</th>
<th>UTS (ksi)</th>
<th>RA (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>B2</td>
<td>1400</td>
<td>131.8</td>
<td>138.9</td>
<td>17.9</td>
</tr>
<tr>
<td>B2</td>
<td>1400</td>
<td>130.3</td>
<td>139.8</td>
<td>17.5</td>
</tr>
<tr>
<td>B1</td>
<td>1500</td>
<td>126.3</td>
<td>134.4</td>
<td>23.9</td>
</tr>
</tbody>
</table>

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3. Rene 95

The two pancakes of cast and wrought Rene 95 used in this program were taken from a vacuum induction melted and vacuum arc remelted ingot approximately 0.228 m in diameter. The alloy composition is given in Table 5. The ingot was given a homogenization anneal in the range 2125°F - 2175°F for four hours and then furnace cooled. The pancakes were subsequently reheated to 2000°F - 2080°F and forged to bring the thickness to 40-50% above the final value. This was followed by a recrystallization anneal at 2125°F for one hour. This results in a uniform grain diameter between .064 - .127mm. The forgings were cooled from the recrystallization temperature at a rate greater than 150°F per hour to 1650°F and then air cooled and taken to final processing. The forgings were reheated to 1975°F - 2025°F and the final reduction was applied, resulting in a further 40-50% decrease in thickness. The pancakes were then partially solutioned at 2000°F, oil quenched to a temperature below 900°F, and aged at 1400°F for 16 hours. This processing resulted in a duplex microstructure consisting of warm worked grains surrounded by a necklace of very fine recrystallized grains.

The Rene 95 forgings have been characterized in terms of microstructure, tensile behavior, and room temperature LEF crack initiation mechanisms. The tensile and creep properties of Rene 95 are summarized in Table 6.
<table>
<thead>
<tr>
<th>Element</th>
<th>Percentage</th>
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<tbody>
<tr>
<td>Nickel</td>
<td>61</td>
</tr>
<tr>
<td>Chromium</td>
<td>14</td>
</tr>
<tr>
<td>Cobalt</td>
<td>8</td>
</tr>
<tr>
<td>Tungsten</td>
<td>3.6</td>
</tr>
<tr>
<td>Aluminum</td>
<td>3.6</td>
</tr>
<tr>
<td>Molybdenum</td>
<td>3.5</td>
</tr>
<tr>
<td>Nichelium</td>
<td>3.5</td>
</tr>
<tr>
<td>Titanium</td>
<td>2.5</td>
</tr>
<tr>
<td>Carbon</td>
<td>0.15</td>
</tr>
<tr>
<td>Iron</td>
<td>0.13</td>
</tr>
<tr>
<td>Silicon</td>
<td>&lt; 0.10</td>
</tr>
<tr>
<td>Manganese</td>
<td>&lt; 0.10</td>
</tr>
<tr>
<td>Zirconium</td>
<td>0.04</td>
</tr>
<tr>
<td>Boron</td>
<td>0.012</td>
</tr>
<tr>
<td>Phosphorus</td>
<td>&lt; 0.01</td>
</tr>
<tr>
<td>Nitrogen</td>
<td>0.003</td>
</tr>
<tr>
<td>Sulfur</td>
<td>6.002</td>
</tr>
<tr>
<td>Lead</td>
<td>&lt; 1.001</td>
</tr>
<tr>
<td>Oxygen</td>
<td>7 ppm</td>
</tr>
<tr>
<td>Silver</td>
<td>&lt; 5 ppm</td>
</tr>
<tr>
<td>Rhenium</td>
<td>&lt; 1 ppm</td>
</tr>
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</table>

*WT I
TABLE 6
AVERAGE TENSILE PROPERTIES OF RENE 95 AT 1200°F

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yield Stress</td>
<td>175 ksi</td>
</tr>
<tr>
<td>Ultimate Stress</td>
<td>210 ksi</td>
</tr>
<tr>
<td>Modulus of Elasticity</td>
<td>25.4 x 10^3 ksi</td>
</tr>
<tr>
<td>% Reduction in Area</td>
<td>12</td>
</tr>
<tr>
<td>% Elongation</td>
<td>11</td>
</tr>
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</table>

RENE 95 CREEP TESTS AT 1200°F

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Stress (ksi)</th>
<th>Secondary Creep Rate (in/in/min)</th>
<th>Time to Failure (min)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C-1-B</td>
<td>130</td>
<td>5.26 x 10^{-4}</td>
<td>94</td>
</tr>
<tr>
<td>C-2-B</td>
<td>171</td>
<td>4.85 x 10^{-5}</td>
<td>433</td>
</tr>
<tr>
<td>C-4</td>
<td>171</td>
<td>6.90 x 10^{-5}</td>
<td>430</td>
</tr>
<tr>
<td>219</td>
<td>160</td>
<td>4.90 x 10^{-5}</td>
<td>960</td>
</tr>
</tbody>
</table>
SECTION III
TEST PROCEDURES

1. SPECIMENS AND EQUIPMENT

Strain-controlled low-cycle fatigue evaluations were performed on two different specimen configurations (see Figure 1). Fourglass-shaped specimens were used with the Rene 95 material and uniform gage length, parallel-sided specimens were used with the AP-115 and AP2-10A materials. All specimens were heated inductively using specially developed induction coils that have been demonstrated to produce very flat temperature profiles within the gage section of the specimen.

Test temperatures were controlled using spot-welded chromel-alumel thermocouples and solid state controllers. The thermocouples were attached just assure that the desired test temperature level and profile were established in the gage section.

In preparing for each test, the specimens were cleaned with Freon and the thermocouples were spot-welded at the proper locations. Then the specimens were connected to the load train and positioned within the induction coil.

For the threaded specimens used in these tests special adapters were employed which contain precision machined flat surfaces for mating with the top and bottom surfaces of the specimen. The buttonhead ends of the adapters were mounted in the specimen holding fixture on the test machine using a split collet type of assembly. Buttonhead specimens were loaded directly into these fixtures. A leveling device was employed to assure that the specimens were installed perpendicular to the platen on the machines. Before any load was applied to the specimen, a visual inspection of the final load train connection was made. This was done by comparing the alignment and parallelism of two closely spaced, precision ground, flat surfaces before they were bolted together. In this
Fig. 1  Test Specimen Designs Used in this Study
manner, the specimen alignment in each and every specimen installation was checked prior to the test. The final bolting operation was performed with the system in load control so that the specimen was not subjected to any extraneous forces during this final assembly operation.

At this time the extensometer was attached to the specimen. For the hourglass-shaped specimens, the diametral extensometer was attached to the minimum diameter which automatically established the gage section. For the uniform gage specimens, a previously established electronic calibration was used to position the extensometer tips over a length that would yield a gage section of exactly 0.500 inch when the specimen was heated to test temperature.

Before any hourglass specimens were tested, the analog strain computer was calibrated by making use of the specimen cross-sectional area (A) and the value for Young’s Modulus (E) at the intended test temperature. The values of A and E were used as shown in the block diagram in Figure 2 to generate axial strain values corresponding to measured values of diametral strain and force. This diagram provides an aid to an understanding of the computer calibration procedure which is based on using the values of A and E and adjusting the compliance control to establish the following equality:

\[ \Delta e = \frac{F}{c_e} \]  

(1)

Prior to heating a specimen to the desired test temperature, the system was placed in force control. This automatically kept the force at zero by gradually lowering the movable platen to account for the thermal expansion of the specimen as the temperature was increased. When the test temperature was obtained, the calibration of the analog strain computer was continued. The specimen was cycled elastically and the inelastic strain output was set to zero. This procedure established the correct value for Poisson’s ratio elastic, \(\nu\), and calibrated the inelastic strain signal with hourglass specimens. The same procedure was used
FIG. 2. Schematic Diagram of Operation of Computer used in Strain control testing.
to calibrate the inelastic strain signal when uniform gage specimens were tested. At this point, the computer was completely calibrated and capable of furnishing the strain components of interest.

Two strip chart recordings were made during start-up, one of the axial force on the specimen and the other of the total axial strain. In addition, a X-Y recorder was used to plot the initial hysteresis loops. The system was placed in number strain control keeping the force at a minimal level by using a by-pass valve. The desired cyclic strain was then gradually established in the specimen. After all final manual adjustments were made to the test machine, the test conditions were automatically held constant until failure.

Hysteresis loops were obtained on the X-Y recorder during the first few cycles and at frequent intervals thereafter. In addition, a continuous recording was made of the applied force and the associated inelastic strain.

After failure occurred, determined either by complete specimen separation or some pre-determined stage of specimen cracking, the shut-down circuit automatically de-energized the entire system including the hydraulic solenoid, induction generator, timing device, cycle counter, and recorders.
2. WAVEFORMS

Various waveforms were used in the course of this data generation program. The majority of specimens, however, were tested using continuous cycling (triangular waveform) and simple strain hold cycles. The continuous cycling tests were run at frequencies of 20 cycles per minute (cpm), 0.2 cpm, and 0.05 cpm. A schematic of this waveform is shown in Figure 3. The simple strain hold cycles included hold times in tension, compression, and tension and compression. These waveforms are also shown in Figure 3 and the nomenclature is further explained in Table 7.

A limited number of tests was also performed on Rene 95 using less conventional waveforms including SLOW-FAST and FAST-SLOW cycling and unsymmetrical strain holds. These waveforms are also illustrated in Figure 3 and further described in Table 7.
### TABLE 7

**DESCRIPTION OF FATIGUE CYCLES AND NOMENCLATURE**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>20 cpm, 0.2 cpm, 0.05 cpm</td>
<td>Continuous cycling at a frequency of 20 cycles/min, 0.2 cycles per minute, and 0.05 cycles per minute.</td>
</tr>
<tr>
<td>1-0</td>
<td>1-min. hold time at maximum strain in tension. 20-cpm ramps for the strain reversals.</td>
</tr>
<tr>
<td>10-0</td>
<td>As in 1-0, except 10-min. hold time instead of 1 min.</td>
</tr>
<tr>
<td>0-1</td>
<td>1-min hold time at maximum strain in compression. 20-cpm ramps for the strain reversals</td>
</tr>
<tr>
<td>0-10</td>
<td>As in 0-1, except 10-min hold time instead of 1 min.</td>
</tr>
<tr>
<td>1-1</td>
<td>1-min hold time at maximum strain both in tension and compression. 20-cpm ramps for the strain reversals.</td>
</tr>
<tr>
<td>10-10</td>
<td>As in 1-1, except 10-min hold time instead of 1 min.</td>
</tr>
<tr>
<td>20-2.05 cpm</td>
<td>Continuous cycling at two frequencies. The positive strain rate was 20-cpm and the negative strain rate was 0.05-cpm. The changes in strain rate occurred at the peak tensile and compressive strains.</td>
</tr>
<tr>
<td>20-1/2-0.05 cpm</td>
<td>As in 20-0.05-cpm, except the change from the fast to the slow strain rate occurred halfway between the peak tensile and zero strain.</td>
</tr>
</tbody>
</table>
### Table 7 (Cont'd)

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05-20-cpm</td>
<td>Continuous cycling at two frequencies. The positive strain rate was 0.05-cpm and the negative strain rate was 20-cpm. The changes in strain rate occurred at the peak tensile and compressive strains.</td>
</tr>
<tr>
<td>0.05-1/2-20-cpm</td>
<td>As in 0.05-20-cpm, except the change from the fast to the slow strain rate occurred halfway between the peak compressive strain and zero strain.</td>
</tr>
<tr>
<td>1-1/2-20-cpm</td>
<td>As in 0.05-1/2-20-cpm, except the slow strain rate was 1-cpm.</td>
</tr>
<tr>
<td>11-0</td>
<td>1-min hold time before the peak tensile strain. 20-cpm ramps for the strain reversals.</td>
</tr>
<tr>
<td>0-11</td>
<td>1-min hold time before the peak tensile strain. 20-cpm ramps for the strain reversals.</td>
</tr>
<tr>
<td>10-1</td>
<td>10-min hold time at the peak tensile strain and 1-min hold time at the peak compressive strain. 20-cpm ramps for the strain reversals.</td>
</tr>
<tr>
<td>1-10</td>
<td>1-min hold time at the peak tensile strain and 10-min hold time at the peak compressive strain. 20-cpm ramps for the strain reversals.</td>
</tr>
</tbody>
</table>
Figure 3 Waveforms and Hysteresis Loops of Fatigue Tests
FAST/SLOW (F/S, 20 - 0.05 cpm)

FAST/SLOW (F/S, 20 - ½ - 0.05 cpm) WITH RATE CHANGE HALFWAY BETWEEN MAX. AND ZERO STRAIN

SLOW/FAST (S/F, 0.05 - 20 cpm)

SLOW/FAST (S/F, 0.05 - ½ - 20 cpm, 1 - ½ 20 cpm) WITH RATE CHANGE HALFWAY BETWEEN MIN. AND ZERO STRAIN

FIG. 3 (Cont'd)
Figure 3 (continued)
RESULTS AND DISCUSSION

1. AP2-1DA

A summary of the test data generated in the evaluation of the alloy, AP2-1DA is presented in Appendix A. These tests employed uniform gauge section specimens tested using axil strain measurement and control. It will be noted that 60 tests were performed, all with an $A$-ratio of unity, with the distribution shown in Table 8.

A semilogarithmic plot of $\Delta \varepsilon$ vs. $N_f$ for the AP2-1DA alloy is presented in Figure 4 to define the behavior at 1400°F for a test frequency of 20 cpm. Within reasonable scatter the data can be represented by two linear segments intersecting near a strain range of 0.73%. This behavior pattern persists to a fatigue life of about 100,000 cycles which represents the range of the experimental data. Beyond this regime the fatigue response has not been defined but it will probably not be represented by an extension of the linear segment defined in the range from 10,000 to 100,000 cycles. It is expected that eventually the data will tend toward an endurance limit and a fatigue life in excess of that corresponding to the linear extension just described.

An overall comparison of all the continuous cycling data is presented in Figure 5. It is to be noticed that the data at 1400°F for a frequency of 0.2 cpm fall very close to the bilinear representation defined in Figure 4 indicating little to no frequency effect over this frequency range. This conclusion should be restricted to the strain ranges tested, however, since no tests were performed below a strain range of 0.70% to determine if this type of frequency response will continue to be exhibited out to 100,000 cycles. A test at 0.2 cpm near a strain range of 0.60 or 3.65% would be needed to complete this definition of frequency response.

\*A - ratio can be used in terms of stress or strain and is defined as the alternating component divided by the mean value, or, mathematically, as: $(\sigma_{max} - \sigma_{min})/(\sigma_{max} + \sigma_{min})$ or $(\varepsilon_{max} - \varepsilon_{min})/(\varepsilon_{max} + \varepsilon_{min})$. 

28
<table>
<thead>
<tr>
<th>Number of Tests</th>
<th>1500°F</th>
<th>1400°F</th>
<th>1200°F</th>
<th>R.T.</th>
</tr>
</thead>
<tbody>
<tr>
<td>20 cpn</td>
<td>7</td>
<td>19(^a)</td>
<td>9</td>
<td>2</td>
</tr>
<tr>
<td>0.2 cpn</td>
<td>4</td>
<td>6</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>4.95 minutes Hold in Tension</td>
<td>1</td>
<td>5(^b)</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>4.95 minutes Hold in Compression</td>
<td></td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1 minute Hold in Tension</td>
<td></td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1 minute Hold in Compression</td>
<td></td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>12</td>
<td>33</td>
<td>13</td>
<td>2</td>
</tr>
</tbody>
</table>

\(^a\) One test was in load control.

\(^b\) One test was a void test.
Another interesting observation associated with Figure 5 involves temperature effects. At 1200°F, the bilinear representation of Figure 4 defines the data at 1200°F fairly well, especially in the life regime beyond 6,000 cycles. At lower cyclic life values the bilinear representation for 1400°F lies just below the data at 1200°F but it would predict the 1200°F data well within a factor of two. Also to be noted, is the absence of a frequency effect at 1200°F which, of course, would be expected since little to no frequency effect was noticed at 1400°F. Finally, the data at 1500°F fall slightly to the left of the bilinear relationship established at 1400°F although there does seem to be a tendency for the fatigue behavior at 1500°F to approach that at 1400°F in the long life regime. This behavior at 1500°F has been approximated by the bilinear construction shown in Figure 5. Included in this construction is a separate dashed line for the data at 1500°F and a frequency of 0.2 cpm. A definite frequency effect is apparent at 1500°F although the effect seems to be well within a factor of two compared to the data at 20 cpm.

In view of the limited number of data points at room temperature no discussion of these results is offered. It will be noted, though, that the two tests that were performed led to fatigue life values that were not significantly greater than those observed at 1400°F (Figure 5).

A limited number of hold-time tests was performed for the AL2-1DA alloy so no extensive conclusions can be drawn. It was noticed that for both the 1-minute and 4.95 minute hold-times, the hold period in compression was more damaging than the hold period in tension. This behavior was also observed for the other alloys and will be discussed in a later section. The hold-period test points are plotted in Figure 6 and compared to the bilinear plot of Figure 4. It can be noted that the 1-minute hold period in compression at a strain range of 1.0% leads to a fatigue life that is about 40% of the continuous cycling value for this strain range. This is about the same amount of fatigue life.
reduction obtained with a 4.95 minute hold period in compression at a strain range of 0.85%. This result is somewhat unexpected although it might represent a saturation effect for hold-time damage. More test information will be needed in order to confirm this tentative interpretation. At 1200°F no hold-time effect is evident since the fatigue life with 4.95 minute hold times was found to be essentially identical to the continuous cycling fatigue life.

Cyclic stress-strain behavior for the AF2-1DA alloy, based on half-life information, is presented in Figures 7 and 8. A comparison with the limited room temperature data is included in each figure as is the effect of frequency. Frequency is seen to have little effect at 1200°F and a small but noticeable effect at 1400°F and 1500°F.

A plot of the AF2-1DA data at 1600°F is shown in Figure 3 where a well-defined linear relationship between log \( \log N \) (based on \( N_f/2 \) information) and \( \log N_f \) is noted. This linearity persists over the range from about 200 to 100,000 cycles and exhibits a slope of approximately -0.32. Data for the other test temperatures are presented in Figure 10 and compared to the linear relationship described in Figure 9. It appears reasonable to represent the data at each temperature with a straight line having the same slope as that assigned in Figure 9, although at 1500°F a definite break in the linear trend seems to develop based on the point near 130,000 cycles. Converting the stress range data of Figures 9 and 10 to elastic strain range by dividing by the elastic modulus provides for some degree of correlation of the temperature dependence noted in Figure 10. This result is shown in Figure 11 based on an average modulus value from the data shown in Appendix A. While this type of plot provides for some normalization of the data a very definite temperature effect is still noticeable as indicated by the lines drawn to represent that data for the temperatures involved. Some further correlation of the temperature effect is
Figure 8:
Stress Range vs Strain Range
AF2-1DA
A = +1.0, 1400°F and R.T.
warranted and a logical approach might be that offered in the Universal Slopes equation where the elastic strain range is represented in terms of the ultimate tensile strength divided by the elastic modulus. It is recommended that this evaluation be performed in a subsequent analysis of these results.

In Figure 11 the two available data points at 1200°F and a frequency of 0.2 cpm indicate no effect of frequency on fatigue life. At 1400°F a small frequency effect appears to be developing. Data at 1500°F are presented in Figure 12 to identify the development of a definite frequency effect as the frequency is reduced from 20 to 0.2 cpm. Additional data will be required to determine if this type of effect is still present in the lower strain range regime (for example, at the point corresponding to a fatigue life of 130,000 cycles at 20 cpm).

An evaluation of the plastic strain range results lead to the plot shown in Figure 13. In the regime near 10,000 cycles the value of the plastic strain range approached 0.01%. At such levels, the reliability for these values is low and it becomes difficult to establish a dependable relationship between plastic strain range and fatigue life. For this reason, only those tests were included in Figure 13 that had plastic strain range values greater than 0.02%. Based on the data at 1200°F, 1400°F, and 1500°F, a series of parallel lines represents the behavior pattern fairly well, for this limited range of fatigue life. It is also noted that the slope of the line defined by the data at 1200°F is very close to a value of -1.0. Lines having this same slope have been drawn at 1400°F and 1500°F and predict the data within a factor of ±2. This slope of -1.0 represents a more negative value than that associated with the Coffin-Manson relation. A slope of -1.0, of course, establishes a unique relationship between $\Delta \varepsilon_{p}$ and $N_f$ in the form:

$$\Delta \varepsilon_{p} \times N_f = \text{constant}$$

(2)

Intercept calculations in Figure 13 lead to values for this constant of 74, 110, 36

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and 135 for test temperatures of 1200°F, 1400°F, and 1500°F respectively. These values will be discussed again in a later section dealing with similar data for Rose 95.
AF-115 was tested in much the same way as the AF2-1DA alloy. Uniform gage section specimens were employed and the tests were performed using axial strain measurement and control. Further more, the test temperatures were essentially the same as those employed in the evaluation of the AF2-1DA alloy and, with one exception, the A - ratio (on strain) was equal to unity. The evaluation of frequency and hold-period effects was also patterned after that followed in the study of the AF2-1DA alloy. A summary of the results obtained in the 100 tests performed in the evaluation of the AF-115 alloy is presented in Appendix B. These tests correspond to the distribution shown in Table 9.

There were two processing conditions of the primary heat of AF-115, HIP and HIP plus forge. The LCF behavior for both conditions was approximately the same as shown in Figure 14. In addition, some specimens from a second heat of AF-115, identified in Appendix B as pancake 3, (300 series), were also tested and their fatigue behaviors were also similar (Figure 14). Since the fatigue responses of the different conditions of AF-115 were approximately equal, these tests will be treated as one population in this analysis.

A semilogarithmic plot of $\Delta e$ versus $\sigma$ for the AF-115 alloy at 1400°F and a frequency of 20 cpm is shown in Figure 15. The bilinear representation for the AF2-1DA alloy from Figure 4 is also included in Figure 15 for comparison purposes. It will be noted that the behavior patterns for the two alloys are quite similar.

All the data in Figure 15 have been combined with the AF-115 data at 1400°F and a frequency of 0.2 cpm to yield the plot shown in Figure 16. In analyzing these results, there was no significant frequency effect on fatigue life at this
<table>
<thead>
<tr>
<th>Number of Tests</th>
<th>1200°F</th>
<th>1400°F</th>
<th>2000°F</th>
<th>2500°F</th>
</tr>
</thead>
<tbody>
<tr>
<td>20 rpm 1 cpmin</td>
<td>12</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>1 rpm 0.2 cpmin</td>
<td>2</td>
<td>2</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>4.95 minutes</td>
<td>9</td>
<td>22</td>
<td>4</td>
<td>2</td>
</tr>
</tbody>
</table>

1. Tests performed in an argon environment using constant axial strain control.
2. Includes one test with A-ratio (on strain) of infinity and one test in load control at 60 cpmin.

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Figure 15
Strain Range vs Nf
AF-115
1000°F A = +1.3

From Figure 4
For AF2-10A
temperature. It was also noted that within reasonable scatter the entire data set could be represented by a straight line (the point at 130,000 cycles is an obvious exception to this linear data trend and, in the absence of further testing in this strain range regime, should probably be viewed as an unusually long fatigue life for a strain range of 0.50%). This line in Figure 16 was used in Figure 17 to provide a comparison of the temperature effect identified in these tests of the AF-115 alloy. Even though the data scatter is quite substantial, a definite temperature dependency is noted and it appears reasonable to represent the data with the linear and parallel isotherms that are shown. Each line can be described by an equation of the form:

\[ N_f = A e^{-b \Delta t} \]  (3)

and since the slopes are the same, the value of "b" is independent of temperature. An extension of this analysis led to an evaluation of the temperature dependency of the value of A in Equation 3 and this led to the following:

\[ N_f = 8150 e^{\frac{8580}{1080} - 7.1 \Delta t} \]  (4)

This expression has been used to position the lines in Figures 16 and 17, and within the limits of the data, provides a good description of the data at 20 cpm, being within a factor of 2 in most instances. Of course, since no frequency effect is observed at 1200°F and 1400°F, this equation can also be applied over the frequency regime from 0.2 to 20 cpm at these two temperatures. At 1500°F, a frequency effect (see points in Figure 17) is observable and some reduction in life is noted as the frequency is reduced from 20 to 0.2 cpm.

It is to be emphasized that Equation 4 was developed using data corresponding to an A - ratio (on strain) of unity and should not be applied at any other A - ratio. Although Equation 4 will probably yield reasonable...
estimates of fatigue life for an A - ratio of infinity in the regime of high strain ranges, it can be expected to underestimate the fatigue life as the one word strain range is reduced. For example, the test of Spec. 2-16 led to a fatigue life of 285,877 cycles at 1400°F, \( \Delta e_c = 0.53\% \), 20 cpm and \( A = -1 \). This life is substantially longer than the value of 16,500 cycles that is obtained from Equation 4 for these conditions at \( A = +1.0 \). Some additional studies would be needed before a term for A - ratio effects could be introduced into Equation 4.
As indicated in Table 8, only 12 hold-time tests were employed in this evaluation of the AF-115 alloy. For this reason, nothing more than trend behavior was identified. A comparison of the results obtained at 1400°F is presented in Figure 18. Within the scatter of the continuous cycling data the hold periods in tension (both 1 minute and 5 minutes) indicate no reduction in fatigue life due to the presence of a hold period. As a matter of fact, there is some indication that hold periods in tension actually lead to an increase in fatigue life. However, a factor of two reduction in fatigue life results when a hold period of 1 or 5 minutes is imposed in compression. This behavior is quite similar to that noted in the tests of the AF2-1DA alloy and again, hold periods in compression appear to be more damaging than periods in tension. At 1500°F only two hold-period tests were performed (both 5-minute hold periods in tension) and the effect is essentially the same as that noted at 1400°F for tension hold-periods.

Cyclic stress-strain behavior for the AF-115 alloy at 1400°F is shown in Figure 19 for the two frequencies employed in these evaluations. As will be noted, no frequency effect appears evident at this temperature. A similar conclusion regarding frequency effect follows from the data shown at 1200°F in Figure 20. At 1500°F, however, the data shown in Figure 20 reveal a noticeable development of a frequency effect. The effect, however, is mild and is seen to amount to about a 10% reduction in stress range as the frequency is reduced from 20 to 0.2 cpm. A comparison of the cyclic stress-strain behavior for the AF-115 material with that for the AF2-1DA alloy in Figures 7 and 8 indicates very similar behavior although the small frequency effect noted at 1400°F in Figure 8 is not observed in Figure 19.
Figure 18
Total Strain Range vs Nf
AF-115
1030°F  A = +1.0

I - Tensile Data
C - Compressive Data

Line from Figure 16
1450°F Continuous Cycling Data

Np, Cycles to Failure
Figure 19
Stress Range vs Strain Range
AF-115
1400°F  A = +1.0

- ○ 20 CPM
- ○ 0.2 CPM
An analysis of the stress range (at $N_f/2$) data for the AF-115 alloy at 1400°F led to the plot of $\log N_o$ versus $N_f$ shown in Figure 21. This result is very similar to that noted in Figure 9 for the AF2-1DA alloy. Within reasonable scatter, the plot is linear over almost three orders of magnitude and the slope of this linear relation is close to -0.14. As in the case of the AF2-1DA alloy, the data in Figure 21 show a negligible effect of frequency at 1400°F over the range from 0.2 to 20 cps. A dashed line has been included in Figure 21 based on the relationship identified for the AF2-1DA alloy in Figure 9. This comparison reveals that the two alloys exhibit very similar stress range versus fatigue life relationships.

Another similarity exists in the temperature dependence exhibited by the two alloys. In Figure 22, the AF-115 relationship from Figure 21 is positioned to provide a comparison of the AF-115 results at 1400°F with data obtained at 1200°F and 1500°F. Linear and parallel isotherms provide a reasonable representation of the data and this behavior pattern is very similar to that noted in Figure 10 for the AF2-1DA alloy. It should also be noted in Figure 22 that the effect of frequency becomes apparent at 1500°F. This, too, is similar to the behavior pattern observed for the AF2-1DA alloy.

A different representation of the stress range data shown in Figures 21 and 22 is provided in terms of elastic strain range in Figures 23 and 24. As should be expected, the behavior patterns noted are identical to those noted for the stress range behavior. In Figure 23, for example, the line drawn to represent all the data at 1400°F reflects the same type of result discussed in connection with Figure 21. Also, the result in Figure 24, associated with parallel isotherms and the development of a frequency effect at 1500°F, is identical to that identified for the stress range behavior of Figure 22.

56
Figure 21
Stress Range vs N
AF-115
14/30°F
A = -1.0

57

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The plastic strain range behavior for the AF-115 alloy is not as well
defined as that for the AP2-1DA alloy even in the range below 10,000 cycles.
However, based on the data available (Figure 25) some general comments
can be made. At 1500°F, and to some extent at 1400°F, the shorter fatigue
life (below about 2000 cycles) results appear to define the same type of
linearity (i.e. slope of -1.0) noted in Figure 13. It will be noted,
though that this persists to a fatigue life value that is far below that
observed at 1500°F (and 1400°F) in Figure 13. Furthermore, the estimated
isotherms for 1400°F and 1500°F in Figure 25 are positioned noticeably
to the left of the corresponding isotherms for the AP2-1DA alloy. Beyond
the life regime of about 2000 cycles the plastic strain range vs. Life
relationship appears to be defined by a line (or curve) having a very
shallow slope. This aspect of the fatigue characteristics of the AF-115
alloy appears to warrant additional study.
With the exception of four tests at 1300°F, all the low-cycle fatigue evaluations of the Rene 95 alloy in this program were performed at 1200°F.

The total effort on Rene 95 at Mar-Test Inc. involved 101 individual tests. (Appendix C) It is also to be noted, that, except for one test (Spec. No. 46), all the low-cycle fatigue evaluations employed hourglass-shaped specimens and computed axial strain control. In this way, then, these tests differed from those performed in the evaluation of the AF2-1DA and AX-115 alloys.

Another difference is related to the $A -$ ratio (on strain) employed.

In the Rene 95 tests, the $A -$ ratio was equal to infinity in most cases except for one test at $A = +1.0$, one test at $A = -1.0$, and a series of six tests in which $A -$ ratio values of $+1/3$, $-1/3$, $+1/5$, and $-1/5$ were investigated.

In addition, a series of special waveforms was evaluated using selected versions of slow-fast and fast-slow cycling. A final observation relating to the Rene 95 evaluations concerns hold-time effects as these were investigated in much more detail than they were in the case of the two other alloys.

An evaluation of the low-cycle fatigue behavior of the Rene 95 alloy in terms of total strain range is presented in Figure 26. A well-defined curvature on this semilogarithmic plot describes the behavior at 1200°F over the range from 200 to about 400,000 cycles. Also to be noted is an apparent approach toward an endurance limit in the strain range regime near 0.8%. Also, at 1200°F a slight frequency effect is noted. As the frequency was reduced from 20 to 0.05 cpm a life reduction factor of approximately 2.0 was realized over the range studied. Tests in the strain range regime near 0.9% are needed to develop an understanding of this behavior.

Another point to be made in connection with Figure 26 concerns temperature effects. While only a few data points are available at 1300°F, it appears that there is a reduction in life with increased temperature. These
Figure 26
Strain Range vs $N_f$
Rev 95

1200°F $A = \infty$

- ○ 29 CPM
- △ 0.05 CPM
- □ 1300 0.05 CPM
- △ $A = -1.0$, 20 CPM
- ◇ $A = +1.0$, 20 CPM
tests at 1300°F also suggest that a reduction in the endurance limit will be encountered as the temperature is increased from 1200°F to 1300°F.

Two data points at 1200°F for an $A - \alpha$ ratio other than infinity are included in Figure 26; one for $A = +1.0$ and one for $A = -1.0$. At a strain-range of 1.2% only a small effect on fatigue life is noted. For $A = +1.0$, a small reduction in life is noted while at $A = -1.0$, a small increase in life is observed. These effects are small, however, and might well be within the range of reasonable scatter for data at $A = \infty$. In any case, no generalizations can be proposed based on these limited results since in the regime of lower strain ranges (0.80% for example) the use of $A = +1.0$ would be expected to lead to significant reductions in life compared to the data at $A = \infty$.

An interesting comparison of the low-cycle fatigue characteristics at 1200°F for the three alloys studied in this program is provided in Figure 27. This comparison can become particularly informative when interpreted in terms of the different $A - \alpha$ ratios involved ($A = \infty$ for Rene 95 and $A = +1.0$ for AF2-LDA and AP-115 alloys). It was pointed out in the discussion of Figure 26 that tests at an $A - \alpha$ ratio of unity and a strain range of 1.2% gave a fatigue life at 1200°F that was not too different (just slightly lower) from that observed at $A = \infty$. Therefore, in this regime of strain range values, the curve for Rene 95 at 1200°F would apply equally well for $A = \infty$ and $A = +1.0$. Furthermore, it is to be noted, that in this strain range regime (about 1%) the isotherm for the Rene 95 alloy at 1200°F is nearly parallel to the 1200°F isotherm for the AF2-LDA and AP-115 alloys. It can also be seen that in this strain range regime the fatigue resistance (for $A = +1.0$) of the Rene 95 alloy at 1200°F appears to be superior to that of the other two alloys at this temperature. This conclusion should be tempered to some extent because of the different test specimens employed (hour glass for Rene 95 and
uniform gage section for the other alloys). Previous studies of this effect have shown that the fatigue life measured using hourglass-shaped specimens is always slightly greater than that obtained with uniform gage section specimens. In light of this result, the behavior of Rene 95 could be positioned much closer to that for the other two alloys. It would seem, however, that the fatigue resistance of Rene 95 would still be slightly superior to that of the two other materials.

In the strain range regime below 1%, the comparison in Figure 27 shows very large differences in the fatigue life of Rene 95 and the other two alloys. This is due principally to the $A$ - ratio effect inasmuch as the endurance limit, for alloys of this type, always occurs at much higher strain range values for tests at $A = \infty$. It is difficult to project what the actual isochron for Rene 95 would be at 1200°F for $A = 1.0$. It would be interesting to have a few tests performed at $A = 1.0$ for the Rene 95 alloy to directly compare LCF behavior. These tests should also include a few specimens having a uniform gage section in order to define the position of the Rene 95 curve with respect to the AF2-1DA and AF-113 curves when the same specimen design is employed. This comparison of $A$ - ratio effects is an interesting one and will be discussed in some additional detail in a later section of this report.

A study of the effect of hold periods at peak strain on the fatigue life of Rene 95 indicated some interesting patterns. Waveforms with strain hold periods in tension, compression, and both tension and compression (balanced hold) were utilized. While this testing effort focused primarily on hold period durations of one minute, there were a few tests in which ten-minute hold periods were employed. This provided the data to identify the different effects of the two hold-period durations and the effect of the location of the hold period within the cycle. An illustration of the effect of
a one-minute hold period in tension is provided in Figure 28 (abbreviations of the form \(1/10\) are employed to define the waveform time imposed; the number in the numerator represents the tension hold period time in minutes and the denominator represents compression hold time). In general, the effect is negligible over the strain range regime from 0.9% to 2.0%. There are a few points at a strain range of 1.0% to indicate a beneficial effect of the one-minute tension hold period. The two, ten-minute hold-period tests shown in Figure 28 indicate essentially the same effect observed for the one-minute hold period. In summary, for Rene 95 at 1200°F \(A = -\) and at strain ranges of 1.2 and 1.6%, hold-period durations of one and ten minutes in tension have no detrimental effect on the fatigue life. This result might be viewed as being unexpected and for this reason should be studied in more detail in future test programs.

Similar tests at 1200°F with hold periods in compression led to results that were significantly different from those described in Figure 28. This behavior is shown in Figure 29 and indicated that one-minute hold periods do exert a noticeable effect in reducing the fatigue life below that observed in continuous cycling tests at the same strain range. It is also observable in Figure 29 that the detrimental effect of a one-minute duration is increased as the hold-period duration is changed to ten minutes. When a hold-period is employed in both tension and compression, the results for one-minute durations are about the same as for the one-minute hold in compression only. This same type of behavior also seems to follow for ten-minute durations although the reduction in fatigue life is somewhat greater than that observed with one-minute durations.

A more graphic summarization of the hold-time effects noted in this study is provided by a plot of the fatigue life reduction factor as used in
Figure 29
Strain Range vs N_f
Hold Period Results
Rene 95 1200°F A = ∞
ASME Code activities. This factor is simply the ratio of the fatigue life without a hold period to the fatigue life observed when a hold period is employed. For certain waveforms the fatigue life reduction factor exhibited a definite trend toward higher values as the strain range was decreased. An example of this is shown in Figure 30A for (1/1) and (10/10) types of tests. A composite of all the hold-time results is shown in Figure 30B and within reasonable scatter the following trends are identifiable:

1) One-minute hold period in tension has a negligible effect on the fatigue life over the strain range regime from 0.9% to 2.0%.

2) One-minute hold periods in compression and in both tension and compression define a fatigue life reduction factor of 2.0 for strain ranges from 1.8% down to about 1.0%; below 1%, there appears to be a sharp increase in the slope of this trend behavior to suggest more detrimental effects in the lower strain range regime; since this lower strain range regime is in the area of special design interest (i.e., fatigue life values greater than 10,000 cycles) a more comprehensive study of hold time effects in this regime appears warranted.

3) Ten-minute hold periods in compression and in both tension and compression define a trend behavior that begins at a fatigue life reduction factor of about 5.0 in the strain range regime near 1.0%. Here again, a further study of hold-time effect is needed in the lower strain range region.

Some comment should be made at this point regarding the development of different mean stress values in the hold-time tests. A good comparison of such behavior is provided in Figure 31. In the continuous cycling tests at 20 cpm, the absolute value of the compressive stress component is always just slightly larger than the tensile stress component. This behavior is shown in Figure 31 and it will be noted that over much of the strain range regime studied a mean compressive stress of about 5 ksi is exhibited. In the region
Figure 30A

Fatigue Life Reduction Factor vs Strain Range

for (1/1) and (10/1)

Rene 95 1200°F  A = ∞
near a strain range of 1.0%, the compressive mean stress is seen to increase to a value near 10 ksi. This result can be compared with the behavior observed for various hold-period combinations as plotted in Figure 31. For the 1/10 combination (one minute hold in tension only) the mean compressive stress is increased above the continuous cycling value and shows an increase to 40 ksi compression in the low strain range regime. This mean compressive stress is increased even more in the 10/0 combination. For the 0/1 combination (one minute hold period in compression only) the mean stress is close to zero in the high strain range regime and gradually increases to about 10 ksi tension at the lower strain ranges. For 0/10, the mean tensile stress is even higher and would appear to approach 40 ksi in the strain range regime near 1%. Data for the 1/1 and 10/10 combinations are not plotted but are not too different from the continuous cycling behavior. In the case of the 10/1 combination, the mean stress behavior is similar to that exhibited by the 1/0 combination. The effect of hold periods on the LCF behavior of Rene 95 using this same data has been extensively treated in previous AFML Technical Report.\textsuperscript{3,2}
A few tests were performed at 1200°F and a strain range of 1.2% in an evaluation of the effect of $A$ - ratio on fatigue life. To allow for convenient comparison, a summarization of these tests (reported in detail in Appendix C) is as follows:

<table>
<thead>
<tr>
<th>Spec. No.</th>
<th>$A$ - ratio</th>
<th>$N_f$, cycles</th>
</tr>
</thead>
<tbody>
<tr>
<td>66-B</td>
<td>-1/5</td>
<td>4,054</td>
</tr>
<tr>
<td>70-B</td>
<td>-1/5</td>
<td>5,814</td>
</tr>
<tr>
<td>69-B</td>
<td>-1/3</td>
<td>3,532</td>
</tr>
<tr>
<td>37</td>
<td>-1.0</td>
<td>2,126</td>
</tr>
<tr>
<td>67-B</td>
<td>41/3</td>
<td>1,114</td>
</tr>
<tr>
<td>64-B</td>
<td>41/5</td>
<td>752</td>
</tr>
<tr>
<td>36</td>
<td>41/0</td>
<td>1,207</td>
</tr>
<tr>
<td>68-B</td>
<td>$\infty$</td>
<td>2,369</td>
</tr>
</tbody>
</table>

There is a definite trend in these results in that the positive $A$ - ratios lead to fatigue life values lower than the value observed at $A = \infty$, while fatigue life values greater than that at $A = \infty$ are observed for the negative $A$ - ratios. In order to remove the discontinuity associated with $A = \infty$, these results were analyzed in terms of $1/A$ as shown in Figure 32.

An interesting linearity is defined to allow the $A$ - ratio effect at this strain range to be expressed mathematically. This analysis of Figure 32 led to the following expression:

$$N_f = B \cdot e^{-b/A} + 2000 \cdot e^{-0.19/A}$$

(5)

(6)

These constants must be recognized as being dependent upon strain range since the slope (related to $b$) is expected to become more negative as the strain range is decreased. The interesting mathematical form in equation (5) suggests another aspect of the Rene 95 fatigue behavior that warrants additional study.
Figure 32
$N_F$ vs $1/A$
RENE 95

$1230^\circ F$, 20 CPM; $\Delta C_t = 1.2\%$
Two other interesting plots that evolved from this study of A - ratio effects are shown in Figures 33 and 34. While the stress range (at $N_e/2$) was approximately the same for all A - ratio values significant differences were noted in the tensile and compression stress components measured at half-life. These differences are shown in terms of the tensile stress component values (Figure 33) and the mean stress values (Figure 34) based on half-life information and reflect extensive variations. In the case of the $\sigma_1$ plot, the overall curve shape appears to be sigmoidal, and in the A - ratio range near $+1/3$ an asymptotic trend is noted. The $\sigma_1$ value in this regime is close to the 0.2% yield value of Rene 95 at 1200°F. Some further evaluation of this observation is in order. Sigmoidal behavior is also exhibited in the mean stress plot of Figure 34 as mean stress values range from -63 ksi at A = -1/3 to 40 ksi at A - ratio values of 1/3 and 1/5.

Cyclic stress-strain behavior derived from the data in Appendix C is displayed in Figure 35. A small frequency effect appears to be developing in the higher strain range regime but the effect is not well substantiated due to the limited number of test points. Also, a small temperature effect seems to be indicated at 1300°F but here again, the data are too limited to draw any general conclusions.

Stress range data (at $N_e/2$) at 1200°F are plotted versus fatigue life in Figure 36. These results define a linear relationship over the life range to about 10,000 cycles at which point the few data points available suggest a transition to a shallower slope and perhaps the tendency toward an endurance limit. Another interesting feature of Figure 36 involves the data at 1200°F for a test frequency of 0.05 cpm. These results define a slight reduction in fatigue life due to the lower frequency and the data points fall on a line that is parallel to that identified by the data at 20 cpm. Another consistent behavior pattern is identified by the data points at 1300°F as shown in Figure 37. Not only is a linear relationship observed in the higher stress range regime, but
this is parallel to the 1200°F isotherm. Also indicated is the transition to a shallower slope in the regime near 10,000 cycles.

Plots comparable to Figures 36 and 37 are obtained for the data expressed in terms of elastic strain range rather than stress range. Such plots are shown in Figures 38 and 39 where it will be noted that the trend behavior for frequency and temperature effects is similar to that described in Figures 36 and 37. For comparative purposes, the elastic line for the AF21DA alloy at 1200°F (this line is about the same as the elastic line for the AF715 alloy at 1200°F) is positioned in Figure 38. It is interesting that in the regime to about 10,000 cycles, the line for the Rene 95 material closely parallels the line for the AF21DA alloy. For all three materials, then, the elastic strain range lines are parallel, at least over the cycle life regime to 10,000 cycles. It is also to be noted that while the elastic line for the AF21DA material at 1200°F remains linear out to about 40,000 cycles, the line for Rene 95 appears to develop a bilinear behavior near 10,000 cycles.

A plot showing the relationship between plastic strain range and fatigue life is presented in Figure 40. Only data below 10,000 cycles are included since beyond this point the plastic strain range values are 0.01% and less and in this regime, the values are of questionable accuracy. A definite linearity is defined in the range to 10,000 cycles and the slope is close to -1.0. As previously noted this slope is noticeably different from that usually associated with the Coffin-Manson relationship for plastic strain range behavior. Instead of having a slope of -0.5 or -0.6, the Δεp and Nf relation exhibits a slope of -1.0 to yield the following relationship:

$$\Delta \varepsilon_p N_f = \text{constant}$$

An intercept calculation for Figure 40 identified this constant to be 131.0 based on Δεp expressed in percent.
Figure 30
Elastic Strain Range vs Nf
RENE 95
1207°F  A = ∞

20 cycles

0.025 EPM

Line for AFZ3BA at 1200 F
from Figure 11
Figure 39
Elastic Strain Range vs $N_e$
Rene 95

$1300^\circ F$  $A = \infty$  23 cpm
Another interesting evaluation of the hold-time results for Rene 95 stemmed from an attempt to correlate fatigue life with the tensile stress component, $\sigma_t$. One of the first plots that was prepared in this evaluation involved $\sigma_t$ vs $N_t$ on logarithmic coordinates as shown in Figure 41. For the continuous cycling results (at 20 cpm) a linear relationship was defined over the range to about 10,000 cycles. Beyond this point, the data suggested a deviation from linearity and the development of a curvature that was concave upward. Data in this long-life regime are not extensive enough to define the shape of the curve exactly, but some tendency toward an endurance limit appears to be identifiable.

Data for a 1-minute hold period in tension were found to describe an interesting behavior. A linear regime was noted that was essentially parallel to the line defined by the continuous cycling results. Secondly, this linearity persisted for only a short span of fatigue life and when deviation from linearity did occur, it defined a curvature that was opposite to that noted for the continuous cycling results. There is no explanation at the moment for these different patterns, but further study appears warranted.

Test results based on a 10-minute hold period in tension are too few to establish any meaningful conclusion, but for the data points available (see Figure 41) a line parallel to the line for 1-minute hold periods is indicated. Whether this line exhibits a deviation from linearity and a curvature to match the 1-minute hold periods results can not be stated at this time. Certainly, such behavior would be expected, but additional test results must be obtained to substantiate this tentative observation.

A significant result emerged from the use of the plot shown in Figure 41 to compare hold periods in compression. It was noted that in terms of $\sigma_c$, all these points, for 1-minute and 10-minute hold periods alike, fell along the line for the continuous cycling results for 20 cpm. This effect
is shown in Figure 42 and suggests the very interesting conclusion, that when viewed in terms of \( \sigma_T \) the fatigue life is closely related to the time involved with the tension portion of the cycle. This time quantity, designated here as \( \tau_T \), is equal to one-half of the cycle time (or 0.5/\( f \)) in continuous cycling tests, to one-half of the ramping time in compression hold tests, and to one-half the ramping time plus the hold-period duration in tension hold-period tests.

A further evaluation of this concept of \( \tau_T \) was based on hold periods in both tension and compression (1/1, 10/1, 1/10 and 10/10) where the results should be related to the \( \tau_T \) values obtained using the tension hold-period duration. This evaluation was found to be consistent with the interpretation described above. Further support for this concept of \( \tau_T \) was found in the continuous cycling tests at 0.05 cpm in which \( \tau_T \) is 10 minutes. In this instance these results should be comparable to the results obtained with a 10-minute hold period in tension. That this is the case is shown in Figure 43.

Over the region of linearity in Figure 41 the slope is found to be -0.135 to yield the following relationship:

\[
\sigma_T = B N_f^{0.135}
\]  

(7)

Since each line is associated with a specific value for \( \tau_T \) the determination of \( B \) values in terms of \( \tau_T \) led to:

\[
\sigma_T = 27.2 \times (12.1 - \log \tau_T) N_f^{-0.135}
\]  

(8)

for \( \sigma_T \) in ksi and \( \tau_T \) in minutes. Rearrangement leads to:

\[
N_f = 4.22 \times 10^{10} (12.2 - \log \tau_T)^{7.407} \sigma_T^{-7.407}
\]  

(9)

It is significant that the term in parentheses in equations (8) and (9) has the form of the parentheses term in the familiar Larson–Miller parameter.
Whether this is truly significant or not is difficult to determine, but further assessment of the concept would appear to be warranted. Also needed are some additional data to further substantiate this tentative model. For example, further testing at 10-minute hold periods in tension is needed in the longer life region to determine if the assumed linear and parallel behavior is appropriate. It would also be very interesting to extend the testing at 0.05 cpm to determine if the curve shape follows that observed at 20 cpm (see Figure 41). Also informative, would be tests at 2 cpm to determine if these follow this pattern for the 1-minute hold-periods in tension in a certain regime and then follow the curved trend behavior noted at 20 cpm.

While Equation (9) has some interesting features it cannot be recommended for serious consideration because of its applicability to a rather narrow range of fatigue life values. Furthermore, the functional form of Equation (7) can now be recognized as not being capable of accommodating either the slope changes in the continuous cycling results or the different type of slope changes in the tension hold-time results.

One attempt to develop a more effective functional relationship for the data presented in Figure 41 involved the use of the type of semilogarithmic plot shown in Figure 44. This type of plot proved to be useful in that the data for 1-minute tension hold-period tests defined a linear relationship over the entire range of the available results. This type of linearity corresponds to the mathematical form:

$$N_f = B e^{-m \sigma t}$$  \hspace{1cm} (10)

However, this functional form was not completely effective since it did not accommodate the continuous cycling results. As noted in Figure 44 the results at 20 cpm define a relation that is linear and parallel to the line for 1-minute tension hold-period results over a limited life regime, but then the same type of curvature noted in Figure 41 is exhibited. Of course, the test

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results for 1-minute and 10-minute compression hold periods fall close to the
relationship defined by the 20 cpm data just as they did in Figure 42. Furthermore, the continuous cycling data at 0.05 cpm are in good agreement with the
10-minute tension hold-period results similar to the trend observed in Figure 43. These observations led to the conclusion that the concept of \( \tau_c \), cycle time
tension, would again be applicable and a mathematical form was developed to ap-
ply over the linear regions in Figure 44. This form was as follows:

\[
N_f = 4.4 \times 10^5 \tau_c^{-0.263} e^{-0.0465 \sigma_c} \tag{11}
\]

with \( \tau_c \) in minutes and \( \sigma_c \) in ksi.

A limited study was made to provide an additional term in Equation 11 to
describe the curve noted in the continuous cycling behavior. This study iden-
tified the following equation:

\[
N_f = 4.4 \times 10^5 \tau_c^{-0.263} e^{-0.0465 \sigma_c} + 4.2 \times 10^{19} e^{-0.354 \sigma_c} \tag{12}
\]

which is applicable only in the case of continuous cycling tests; for hold-
period tests Equation (11) is to be used.

Actually, Equation (12) must be viewed as tentative since it is based on
very limited test information. For example, as shown in Figure 44, only two
data points at 20 cpm are available for the life regime above 30,000 cycles
and both these are considered "run-outs" (one was a failure in the threads) and
hence do not provide an exact definition of the fatigue life, but rather, a
lower-bound life value. Another limitation on Equation (12) involves the ap-
lication at other frequencies. Additional testing at 0.05 cpm in the longer
life regime will be needed to substantiate the ability of the second term Equa-
tion (12) to accommodate the behavior at another frequency.

To provide some analysis of the effectiveness of Equations (11) and (12)
a series of test conditions from Appendix III was selected and a comparison was
made of measured and estimated values of \( N_f \). This study led to the
Table X - Comparison of Experimental and Estimated Values for $N_f$ for Rene 95 at 1200°F and $A = -$

<table>
<thead>
<tr>
<th>Spec. No.</th>
<th>WAVE FORM</th>
<th>$T_e$ MINUTES</th>
<th>MEASURED $N_f$ CYCLES</th>
<th>ESTIMATED $N_f$, Eq. (11) or (12), CYCLES</th>
</tr>
</thead>
<tbody>
<tr>
<td>22B</td>
<td>0/10</td>
<td>0.025</td>
<td>224</td>
<td>323</td>
</tr>
<tr>
<td>23B</td>
<td>10/1</td>
<td>0.025</td>
<td>224</td>
<td>323</td>
</tr>
<tr>
<td>25B</td>
<td>1/10</td>
<td>0.025</td>
<td>349</td>
<td>213</td>
</tr>
<tr>
<td>26B</td>
<td>1/10</td>
<td>1.025</td>
<td>464</td>
<td>390</td>
</tr>
<tr>
<td>41</td>
<td>0/10</td>
<td>0.025</td>
<td>283</td>
<td>593</td>
</tr>
<tr>
<td>34</td>
<td>0.05 cpn</td>
<td>10.0</td>
<td>526</td>
<td>397</td>
</tr>
<tr>
<td>41B</td>
<td>0/1</td>
<td>0.025</td>
<td>1,940</td>
<td>1,664</td>
</tr>
<tr>
<td>53B</td>
<td>0/10</td>
<td>0.025</td>
<td>1,397</td>
<td>1,634</td>
</tr>
<tr>
<td>19</td>
<td>0.05 cpn</td>
<td>10.0</td>
<td>1,138</td>
<td>1,084</td>
</tr>
<tr>
<td>29B</td>
<td>1/1</td>
<td>1.025</td>
<td>5,277</td>
<td>5,225</td>
</tr>
<tr>
<td>51B</td>
<td>fast/slow</td>
<td>0.025</td>
<td>636</td>
<td>650</td>
</tr>
<tr>
<td>52B</td>
<td>slow/fast</td>
<td>10.025</td>
<td>194</td>
<td>107</td>
</tr>
</tbody>
</table>
results shown in Table X. In general, the agreement is very good and suggests that the concept deserves a more detailed study in subsequent programs.

It is to be recognized that there is some complication involved with the use of Equations (9), (11), and (12) since the fatigue life is expressed as a function of \( q_t \). However, this complication is no more serious than those associated with correlations involving stress range and plastic strain range. An experimental program must provide stress-strain information expressed in terms of the tensile stress component. It should also be noted, however, that the cyclic stress-strain behavior must be described for the various waveforms involved since the stress-strain behavior for continuous cycling tests will probably not be adequate for certain other waveforms. For example, in Figure 45 the data at 20 cpm would not provide a good representation for the other waveforms. Data at 0.05 cpm appear to be close to the 1/10 data, but these all fall below the 20 cpm data. Data for 10/0 fall even lower than the 1/10 and 0.05 cpm results. Finally, 0/1 and 0/10 data fall above the 20 cpm results (fast-slow and slow-fast results are close to the (0/1) data) while 1/1 and 10/10 data are fairly well represented by the 20 cpm data.

If the concept of the cyclic tensile stress is to be developed the trends identified in Figure 45, for use in Equations (9), (11) and (12), need experimental verification. For instance, the behavior for 0/10 can be extended to lower and higher strain ranges by comparison to the other curves, but how accurate this is when used to estimate \( N_f \) values needs to be established in laboratory tests. So do estimates for fatigue life at intermediate frequencies and for longer hold periods (i.e. beyond 10 minutes).
6) Special Discussion of Presentation of Stress Components

Continuous cycling tests at \( A = -1 \) usually exhibit a mean stress close to zero. Such tests were performed in the evaluation of the B-8095 alloy and as noted in the discussion of Figure 31, the compressive and tensile stress components were of nearly equal magnitude. Actually, a small compressive mean stress was found to exist over all the strain range values employed. However, in continuous cycling tests at \( A = 1.0 \), such as were performed for the AF21DA and AF15 alloys, wide variations in mean stress are observed depending upon temperature, strain range and frequency. In these situations, it is important to define the fatigue response completely by some type of graphical presentation of the tensile and compressive stress components. For example, one type of graphical display is presented in Figures 46 and 47, where it is noted that similar behavior patterns are exhibited by the two alloys. In the higher strain range regime, the magnitude of the tensile stress approaches, or becomes equal to, that of the compressive stress to define a region within which the mean stress is close to zero. As the strain range is decreased, the magnitude of the compressive stress falls below that of the tensile stress to yield a region within which a mean tensile stress is exhibited. In the totally elastic regime the compressive stress is essentially zero to correspond to a condition for which the value of the mean stress is equal to one-half the tensile stress (i.e. \( A = +1.0 \) on stress).

Some effect of cycling frequency is noted in Figures 46 and 47. At 0.2 cps the behavior at the high strain range values does not appear to be affected, but at lower strain ranges, the \( \sigma_L \) and \( \sigma_C \) values define a condition, for a given strain range, that is closer to a zero mean stress value than that observed at 20 cps.

Another method for presenting stress component data was identified in this
Figure 47
σT and μ vs ΔE_t
AF-115
1401°F  A = +1.0
program and is illustrated in Figures 48, 49, and 50. In this construction
the stress amplitude ($\Delta \sigma /2$ at $N_f /2$) is plotted as a function of the strain
amplitude ($\Delta e /2$). Also included in this diagram is the elastic line based
on the data in Appendices I and II. This, of course, allows values for pseudo-
alternating stress to be read directly as points along this elastic line. An-
other important feature of Figures 48, 49, and 50 is the inclusion of the
mean stress values to provide a very clear demonstration of how these quanti-
ties vary with strain amplitude. An interesting aspect of this mean stress
behavior is that, for the three figures shown, the variation is not only linear,
but it is linear in each case over the entire strain amplitude regime, from
approximately 0.2 to 0.6%. Another important feature regarding this linearity
in the type of diagram presented here is the separate boundary regions estab-
lished by the intersection of the mean stress line with the stress amplitude
data and with the zero stress axis. Three regions are thereby defined as shown
in Figure 48, 49, and 50. In Region I, $A_\sigma = 41.0$ to indicate that the mean
stress is equal to the alternating stress and can be read as points along the
estatic line for any given strain amplitude; in the Region II, $A_\sigma$ is greater
than 1.0, but less than infinity, and mean stress values can be read from the
mean stress line. Finally, in Region III, $A_\sigma = \infty$, and the mean stress is
zero. An illustration of how the $A - r$ ratio (expressed as $1/A_\sigma$) on stress
varies with strain amplitude for the data in Figure 49 is shown in Figure 51.

Frequency was found to have a definite effect on the position of the mean
stress line although the data are not extensive enough to enable any more than
a qualitative interpretation to be made at this time. Based on a study of the
data for AFT15 at 1400°F and 0.2 cpm, the line terminating in point "p" (Figure
50) has been positioned to represent mean stress behavior at this lower fre-
quency. In the higher strain amplitudes (near 0.60%), the mean stress in near
zero and as the strain amplitude is decreased, the mean stress value increases

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Figure 50
AF-115
1400°F

\[ A = +1.0; \ 20 \text{ cpm} \]

Region I
\[ +1.0 < A_{p} < \infty \]

Region II
\[ A_{p} = +1.0 \]

Region III
\[ A_{p} = \infty \]

Stress at \( P/2 \), ksi

160
120
80
40
0

Stress

Strain

Alternating Stress

Mean Stress

20 cpm

Mean Stress for
0.2 cpm

\[ \Delta \varepsilon \sqrt{2}, \% \]

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in the tension direction but never to values as high as those observed at the higher frequencies. This line has been terminated at point "P" since this represents the limit of the test results. It would be reasonable to assume that this line should continue to be linear and intersect the elastic line near a strain amplitude of 0.1%, but more experimental results are needed for confirmation.

A further development of the stress-strain-amplitude plot, described in conjunction with Figures 48, 49, and 50, is illustrated in Figure 52. In preparing this example, Figure 48 was selected and is positioned in Figure 52 so that the strain amplitude axis is the ordinate. Data in this form were plotted alongside the fatigue results (\(\Delta\sigma\) vs \(N_f\)) of Figure 5 with the applicable stress component information. In this plot then, a complete description is provided for a given alloy tested at a given temperature, A - ratio and frequency. For example, if a certain strain range is selected, the chart given in Figure 52 is entered with the value for the strain-amplitude, and in addition to reading the fatigue life by a horizontal projection to the right, a horizontal projection to the left yields values for stress amplitude (doubling this, yields the stress range) and mean stress. Adding the stress amplitude to the mean stress leads to the value for the tensile stress component. Dividing the stress amplitude by the mean stress, allows the A - ratio on stress to be calculated. If this latter quantity is important in certain applications, the type of plot shown in Figure 51 could easily be added to the left-hand side of Figure 52 to enable this A - ratio value (on stress) to be read directly as \(1/A_o\). Also included in Figure 52 is an average value for the elastic modulus based on measurements made during the start-up of tests in which an axial extensometer is used. This defines the relationship between stress range and elastic strain range, and enables an elastic strain range scale to be positioned in Figure 52. A vertical pro-
jection from a given stress amplitude value yields the corresponding value for the elastic strain range. Then, the associated value for the calculated plastic strain range can easily be obtained by subtracting the elastic strain range from the total strain range. In this plot, a fairly complete definition of material response characteristics is available for a given material at a selected frequency, temperature, and $A_e$ - ratio. Similar plots at other temperatures, $A$ - ratios (on strain) and frequencies would represent a comprehensive description of the fatigue characteristics for a material.

Another observation that has been made in conjunction with Figure 52 relates to the significance of two strain amplitude values on the stress-strain-amplitude plot. One value is associated with the deviation of the stress amplitude data from the elastic line. This is identified as point $X$ in Figure 52 and appears to correspond to the upper slope change in the $N_f$ plot (identified as point $X$ in Figure 52). A second strain amplitude value is associated with the intersection of the mean stress line with the elastic line (identified as point $Y$ in Figure 52). This point has a counterpart on the fatigue plot at $Y$ and should correspond to the location of another slope change at which point the fatigue curve should develop a much shallower slope and tend to exhibit an endurance limit. Admittedly, this interpretation is not completely substantiated experimentally and hence must be viewed as very tentative. It seems, however, to represent an interesting concept and one that should be studied in subsequent programs. Perhaps even a third point could be identified in Figure 52 as the point where the mean stress is zero. However, this too, must await further evaluation.
REFERENCES


1. Relaxed Stress = Stress at beginning of hold period minus stress at end of hold period.

2. Nominal value

3. "±" indicates specimen failed outside the gage section.

4. Load control test - Strain not measured.

5. INTY = infinity

6. Actually 4.95 minute/0 minutes
1. Relaxed Stress = Stress at beginning of hold period minus stress at end of hold period.

2. Nominal value

3. "w" indicates specimen failed outside the gage section.

4. Load control test - strain not measured.

5. INFT = Infinity

6. Actually 4.95 minutes/0 minutes.

7. 200, 400, 700 900C as HIP condition
    300 Heat F1
    500C HIP + forge
1. Nominal values

2. Relaxed tensile stress = tensile stress at beginning of hold period minus tensile stress at the end of the hold period.

3. The stress and strain at the beginning of the hold period for the intermediate hold tests. For the SLO-FAST and FAST-SLOW tests, the stress and strain when the strain rate changed from the fast to the slow rate.

4. INTY = Infinity nominal value

5. Specimen was prestrained to 2% compression and then to zero strain before test began.

6. Uniform cylindrical gage section specimen of 0.25 in. Specimen was preworked by cycling it form zero to 174.4 ksi, back to zero and then to 180.0 ksi and back to zero. This pre-work resulted in a plastic strain of 0.72%. This strain was used as the zero strain level for the fatigue test. This pre-work caused a mean tensile stress to develop in the fatigue test.

7. The axial plastic strain was the controlled variable.

8. Specimen was initially cycled at \( \alpha = 0.97\% \) for 182 cycles using a 0.05-1/2-20 cpm waveform. Since this pre-cycling was not considered damaging the value of \( N_f \) does not include these cycles.

9. Test was stopped and restarted. The stress and strain was measured near 5288 cycles. The large tensile mean stress appears to be an anomaly. Specimen 269 was initially cycled under the same conditions as 2257, but developed a mean compressive stress after 282 cycles.

10. Value not recorded.

11. - failed in threads. Stress and strain measured at 70,212 cycles.

12. - runout. Stress and strain measured at 298,784 cycles.

13. - suffixes mean: I - invalid life

14. - runout

15. - Test was stopped and restarted.

16. - Test was stopped and restarted at 1367 minutes.

17. - Plastic strain not recorded. Value calculated from: plastic strain = total strain minus (stress range divided by the elastic modulus).

18. - Values measured from the hysteresis loop at \( N_f/2 \).