PREPARATION AND PROPERTIES OF MONODISPERSE BRANCHED POLYSTYRENE

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ABSTRACT

Model branched polymers have been prepared by the reaction of relatively monodisperse polystyryl lithium with silicon tetrachloride. The branched molecules have been carefully characterized by light scattering and osmotic pressure measurements. A study of the dilute solution properties of the branched molecules has confirmed the theoretical development of the branching coefficient, g', by Zimm and Killb. The second virial coefficient, A2, has been found to decrease with increased branching. In addition, the Huggins constant, k', has been found to be a poor measure of branching in molecules.

INTRODUCTION

Zimm and Killb have presented theoretical formulas for the intrinsic viscosity and viscoelastic properties of some model branched molecules in dilute solution. Using their theoretical expression, they were able to calculate the ratio of the intrinsic viscosities of several model branched molecules to that of linear molecules having the same molecular weight. This ratio is expressed by the following equation,

$$g' = \frac{[\eta]_b}{[\eta]}$$

Although they referred to data available in the literature to substantiate the validity of their work, the inherent uncertainties in the branched polymer characterizations detracted from the test of the mathematical treatment.

In order to resolve this uncertainty, it was the purpose of this work to prepare well-characterized model branched polymers and study their dilute solution behavior. The unique characteristics of anionic polymerization lend themselves very well to the purpose intended. The anionic polymerization of styrene can be used to prepare relatively homogeneous linear polymer of predetermined molecular weight. In addition, the "living" nature of the polystyryl anion can be used to further advantage in the preparation of the branched molecules. In this work, the polystyryl anion was reacted with silicon tetrachloride to yield molecules with three and four uniform branches emanating from a single point. These "star" type molecules were then used to experimentally
determine the g' factor, the second virial coefficient, A₂, and the Huggins constant, k'.

EXPERIMENTAL

Preparation of Linear Polystyrene

In order to prepare model branched compounds consistent with the models used in the calculations of Zimm and Kirk, it was necessary to prepare relatively monodisperse linear polystyrene. To accomplish this task, styrene monomer was polymerized using anionic polymerization techniques under high vacuum (10⁻⁸ mm Hg). The details concerning purification of solvent and monomer and the use of catalyst seed have been described elsewhere. The polymerization apparatus is shown in Figure 1 and the procedures used, with exception of one modification, have already been described. The modification consisted of distilling the styrene monomer from the ampoule into the frozen benzene seed solution in flask F₁ (see Figure 1). This distillation insured the addition of pure monomer to the reaction flask, whereas the freezing of the mixture prevented polymerization during distillation. After thawing, the monomer-seed solution was thoroughly mixed and a substantial portion was transferred to flask F₂. Having transferred some of the solution, flask F₂ was cut away. The solutions in both flasks were kept at room temperature for 24 hours with continuous stirring. The polymerization was considered complete after the 24 hour interval.

In order to determine the molecular weight of the linear polymer prepared in this manner, the catalyst concentration of the polymer in flask F₁ was determined by titrating the orange colored polystyryl anions with a standard n-butanol solution by means of a slow-leaking burette, B (see Figure 1). The butanol termination of the polystyryl anions caused a loss of color, and thus the titration end-point was a colorless solution. After titration, the polymer was precipitated from solution with methanol, filtered, dried and weighed. Hence, from the weight of polymer and the number of moles of catalyst, it was possible to estimate the molecular weight of the linear polymer. This linear polymer is referred to as the S₁₀ sample.

Preparation of Branched Polystyrene

The polymer remaining in flask F₁ was used to prepare the branched molecules. Knowing the amount of monomer initially used, and the weight and molecular weight of the polymer in flask F₁, it was possible to calculate, by difference, the number of moles of polymer in flask F₂. To this flask was added a less than equivalent amount of silicon tetrachloride calculated on the assumption that all four chlorines would be replaced by polystyryl anions. The excess of polystyryl anions was necessary to insure that the linking reaction would go to completion.

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The silicon tetrachloride used in the linking reaction was treated in the following manner. It was dried over anhydrous sodium sulfate and distilled twice before collecting into weighed ampoules. Benzene solutions were made and the concentration of silicon tetrachloride was determined by breaking an ampoule in ice water and titrating the liberated hydrochloric acid with standard sodium hydroxide solution using phenolphthalein as an indicator.

Having introduced the silicon tetrachloride into the polymer solution, the mixture was allowed to stand for 48 hours at 50°C. At the end of this period, any remaining polystyryl anions were terminated by the addition of n-butanol. The resulting polymer mixture was precipitated in methanol, dried, and weighed. This polymer sample is referred to as the 4S15 sample.

Polymer Characterization

The polymer sample 4S15, which was the total polymer product of the linking reaction of polystyryl-lithium and silicon tetrachloride, was initially expected to contain the tetra-linked star molecules and the excess linear polymer S15. Hence, fractionation was considered necessary to isolate the pure, linked product. However, careful fractionation became even more important when, in initial attempts at preparing the linked products, it was observed that mixed products of tetra- and tri-linked molecules were being formed.

Fractionation

The mixed polymer product, 4S15, was dissolved in benzene to give a 0.12% solution by weight. The non-solvent used for the fractionation was methanol. The fractionation was carried out at a constant temperature of 30°C. Upon separation, the fractions were precipitated in methanol, dried in vacuo, and weighed. The weight fraction data for the fractionation are listed in Table I.

Molecular Weight Determinations

In order to establish the efficiency of fractionation, the degree of linking and the homogeneity of both linear polymer and the fractions, it was necessary to determine both the weight- and number-average molecular weights of the samples. To obtain this information, osmotic pressure and light scattering measurements were made.

The light scattering measurements were made using a Bric-Phoenix light scattering photometer, Universal 1000 series. Calibration was accomplished through the use of a reference standard opal provided with the instrument. In order to recheck the calibration, the absolute turbidity of benzene was determined, and it agreed to 0.6% with the value listed by Carr and Zimm. All the solutions were filtered through sintered glass frits to remove insoluble impurities. The scattering intensities of the solutions
were determined at various angles through the use of a cylindrical cell having the dimensions, 75 x 26 mm. The scattering system was a polystyrene-benzene solution and the refractive index increment for a wave-length of 436 millimicrons was 0.1151 ml gm⁻¹. The data obtained were interpreted through the use of a Zimm plot. The weight-average molecular weights thus obtained are listed in Table I.

The number-average molecular weights were obtained through osmotic pressure measurements. The osmometers used were of the design developed by Immergut and Stahl². The membranes used were gel cellulose, grade No. 500. The osmotic molecular weight of the linear \( S_1 \) sample was determined in benzene solution at 30°C. For fractions, A-4S10 and B-4S10, the measurements were made in butanone at 25°C. All the osmotic pressures were obtained by the static method and the equilibrium times were of the order of 20 hours. The number-average molecular weights are listed in Table I.

**Viscosity Determinations**

In order to obtain \( \eta' \), it was necessary to experimentally determine the intrinsic viscosity of the branched molecules. The viscosities were determined in two solvents, toluene at 25°C and cyclohexane at 34°C, the former being a good solvent and the latter a theta, \( \theta \), solvent. The measurements were made using a Ubbelohde dilution viscometer having a flow time of 123 sec. for toluene and 193 sec. for cyclohexane, and having a negligibly small kinetic energy correction.

**RESULTS AND DISCUSSION**

The fractionation data and weight-average molecular weight values are listed in Table I. The agreement between the weight-average molecular weight of 4S10 which was determined experimentally to be 1.93 x 10⁶, and the calculated value of 1.90 x 10⁶ for this sample calculated from the data for the individual fractions, indicates that the fractionation was efficient and complete. However, to insure that the fractions were homogeneous, number-average molecular weights were determined (see Table I) and were used to determine the heterogeneity ratio, \( M_n/M_w \), for the A-4S10 and B-4S10 samples. In addition, the heterogeneity ratio was determined for the linear \( S_1 \) sample. The ratios obtained indicated that the fractionation was indeed very efficient and that both fractions of the linked polymer and the linear polymer were homogeneous enough for the purposes intended.

Having established the fact that homogeneous fractions were obtained, it was still necessary to determine the degree of branching that had taken place to produce each fraction. This was done by calculating the linking ratio, i.e., the number-average molecular weight of the branched molecule divided by the number-average

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TABLE I

Fractionation and Molecular Weight Data

<table>
<thead>
<tr>
<th>Sample</th>
<th>Weight Fraction</th>
<th>$\bar{M}_w$ x $10^5$</th>
<th>$\bar{M}_n$ x $10^5$</th>
<th>$\bar{M}_w$</th>
<th>4$\bar{M}_w$</th>
<th>$S$-$\bar{M}_w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{10}$</td>
<td>-</td>
<td>0.606</td>
<td>0.574</td>
<td>1.06</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>4$S_{10}$</td>
<td>-</td>
<td>1.93</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>A-4$S_{10}$</td>
<td>0.252</td>
<td>2.57</td>
<td>2.35</td>
<td>1.09</td>
<td>4.09</td>
<td></td>
</tr>
<tr>
<td>B-4$S_{10}$</td>
<td>0.349</td>
<td>1.70</td>
<td>1.70</td>
<td>1.00</td>
<td>2.96</td>
<td></td>
</tr>
</tbody>
</table>

molecular weight of the linear sample, $S_{10}$, i.e., $4S_{10}$-$M_2/S_{10}$-$M_1$. The reasons for using the number-averages to determine the degree of linking are given in the Appendix, where the effects of molecular weight distribution are considered. In the case of the A-4$S_{10}$ sample, the ratio was, within experimental error, 4.0, whereas for B-4$S_{10}$ the ratio was 3.0, as shown in Table I. Thus, having shown the linear polymer to be relatively homogeneous, and having demonstrated the separation of homogeneous branched polymers it can be assumed that the A-4$S_{10}$ sample is a "star" type molecule with four branches, of essentially the same length, emanating from a single point. The B-4$S_{10}$ sample is a "star" with three such branches.

Viscosity measurements were made for both branched polymers in toluene at 25°C, a good solvent, and in cyclohexane at 34°C, the theta solvent. The data are listed in Table II. In order to determine the branching coefficient, $g^*$, as defined by Zimm and Kibb, it was necessary to obtain the intrinsic viscosity of a linear polymer having the same molecular weight as each of the branched polymers. It was originally intended to calculate these values using the viscosity-molecular weight relationship reported by Outer, Carr and Zimm for polystyrene-toluene at 25°C. However, the linear polymer prepared by anionic polymerization in benzene did not exactly obey the equation reported by Outer, Carr and Zimm. The viscosities experimentally determined were observed to be consistently lower than those calculated from the literature equation. Therefore, it was necessary to establish the viscosity-molecular weight equation experimentally. The equation determined for toluene at 25°C was as follows,

$$[\eta] = 1.46 \times 10^{-4} M_w^{0.69}$$

The reason for the slight difference between this equation and that reported by Outer, Carr and Zimm is unknown at the present time. There is a remote possibility that there is a consistent error in these measurements. However, the procedure used herein eliminates any error in the $g^*$ calculations.

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In order to calculate the viscosity of the linear polymer in cyclohexane at 34°C, it was necessary, due to the discrepancy observed in toluene, to apply a proportionate correction to the viscosity-molecular weight equation reported for cyclohexane at 34°C by Kirkbaum and Flory. The equation determined for these polymers is as follows:

\[ [\eta] = 7.45 \times 10^{-2} M^{0.3} \]

The viscosities calculated, using the above equations for linear molecules of the same molecular weight as the branched molecules, are listed in Table II. The ratios of the branched to linear intrinsic viscosities for both toluene and cyclohexane have been calculated and the agreement between the experimentally and theoretically determined \( q' \) factors is very favorable (see Table III). Thus, within the degrees of experimental error involved, this viscosity study lends considerable support to the theoretical work of Zimm and Kilb.

**Table II**

<table>
<thead>
<tr>
<th>Polymer</th>
<th>[(\eta)]_{Exp}</th>
<th>[(\eta)]_{Calc}</th>
<th>(g')_{Exp}</th>
<th>(g')</th>
<th>Theory</th>
</tr>
</thead>
<tbody>
<tr>
<td>A-4S_{10}</td>
<td>70.5</td>
<td>30.9</td>
<td>37.8</td>
<td>0.84</td>
<td>0.82</td>
</tr>
<tr>
<td>B-4S_{10}</td>
<td>56.3</td>
<td>28.8</td>
<td>30.7</td>
<td>0.90</td>
<td>0.94</td>
</tr>
</tbody>
</table>

\( [\eta] \) - ml gm\(^{-1} \)

\( [\eta]_L \) - linear

\( [\eta]_B \) - branched

*Toluene at 25°C, cyclohexane at 34°C.

The second virial coefficient, \( A_2 \), was obtained for the branched molecules in benzene and butanone. The \( A_2 \) values in benzene were obtained from light scattering data, whereas the values in butanone were obtained from osmotic pressure measurements. The \( A_2 \) values for linear molecules corresponding to the molecular weights of A-4S_{14} and B-4S_{10} were obtained from a plot of the log \( A_2 \) vs. log \( M \) for linear molecules (see Table III). From the data, it can be observed that, in going from linear to branched molecules, the \( A_2 \) value decreases. In addition, this decrease is proportionally greater when the degree of branching is increased. On changing from a good to poor solvent, the \( A_2 \) value is further decreased and, as would be expected, the difference in the \( A_2 \) values for A-4S_{14} and B-4S_{10}, due to branching, becomes less obvious as the second virial coefficient decreases. These results are in agreement with theory and support the corresponding suggestions of Thurmond and Zimm. It can be concluded that the second virial coefficient may be used as a qualitative measure of branching, but only in a good solvent.

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TABLE III
Second Virial Coefficient Data

<table>
<thead>
<tr>
<th>Polymer</th>
<th>Linear $^a$ (Benzene) $A_1 \times 10^3$</th>
<th>Branched Benzene</th>
<th>Branched Butanone</th>
</tr>
</thead>
<tbody>
<tr>
<td>A-4S$_{10}$</td>
<td>0.54</td>
<td>0.33</td>
<td>0.19</td>
</tr>
<tr>
<td>B-4S$_{10}$</td>
<td>0.57</td>
<td>0.49</td>
<td>0.19</td>
</tr>
</tbody>
</table>

TABLE IV
Huggins Constant Data

<table>
<thead>
<tr>
<th>Polymer</th>
<th>Linear $^a$ (Toluene) $k'$</th>
<th>Branched C$_7$H$_8$</th>
<th>Branched C$<em>6$H$</em>{11}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A-4S$_{10}$</td>
<td>0.31</td>
<td>0.38</td>
<td>0.85</td>
</tr>
<tr>
<td>B-4S$_{10}$</td>
<td>0.31</td>
<td>0.41</td>
<td>0.88</td>
</tr>
</tbody>
</table>

$^a$ Determined for linear molecules having molecular weights corresponding to those of the branched polymers.

The Huggins constant, $k'$, was determined for the branched molecules, A-4S$_{10}$ and B-4S$_{10}$, and for linear molecules of the same molecular weights, in toluene at 25°C. In addition, the $k'$ values were obtained in cyclohexane at 34°C for both branched samples (see Table IV). The data obtained indicate an increase in the $k'$ value on going from linear to branched molecules and from good to poor solvents. In spite of this, the value of $k'$ actually decreases when going from the less branched B-4S$_{10}$ to the more branched A-4S$_{10}$. Hence, it appears that $k'$ does not behave in any simple way with degree of branching.

This is not unexpected when one notices that in the equation defining the Huggins constant,

$$\eta = \eta_p/c + k' [\eta]^2/c.$$  

The factor $k'$ $[\eta]^2$ is the proper measure of intermolecular interference at concentration c. The quantity $[\eta]^2$ decreases or increases as the molecule shrinks or grows larger. It is the primary measure of the way in which the molecules will interfere with each other at a given concentration. The factor $k'$ varies only slightly in comparison with $[\eta]^2$ and can be thought of as a correction factor necessary to compensate for small inaccuracies introduced by the use of the simple, but not rigorously correct.
factor $[\eta]^2$. It is to be expected that the variation of $k'$ with branching and solvent power will not be understood until a very accurate theory for the concentration dependence of viscosity is available.

As the data indicate, even in a good solvent, the effect of branching on $k'$ approaches the limits of experimental error. Thus the value of determining $k'$ to establish the degree of branching is very limited. In addition to this fact, a dependence of $k'$ on molecular weight has been reported by Cragg and Sonnalla, and this will further complicate the interpretation of $k'$ values. Thus, because of these various limitations, $k'$ becomes, at best, a very poor indication of the degree of branching.

CONCLUSIONS

The present studies have been successful in clarifying the following points: 1. Branched molecules of accurately determined form can be prepared by the methods used in this study. 2. The theory of Zimm and Kibbel for the intrinsic viscosity of branched molecules is valid. In addition, $q'$ values are nearly the same for both good and poor solvents. 3. The value of the second virial coefficient, $A_2$, is lower for a branched molecule than for a linear molecule of the same molecular weight. This effect is most easily observed in the case of good solvents. 4. Branching is not easily determined by measurement of the Huggins constant, $k'$. Although small changes are observed, they are not easily interpreted.

Since the molecules prepared for this study have been uniform and well characterized, other data in the literature, which may at times conflict with the above conclusions, should be used with caution.

REFERENCES


LEGEND FOR FIGURE 1.

Polymerization Apparatus

A - standard n-hexanol solution ampoule
B - slow leaking burette
C₁ - catalyst seed for purging
C₂ - catalyst seed for polymerization
F₁ and F₂ - flasks with magnetic stirrers for polymerization and linking reactions
F₃ - flask to remove purging solution
M - monomer ampoule
S - solvent ampoule
V - vacuum outlet

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FIGURE 1 - POLYMERIZATION APPARATUS